Neutrino cosmology: measuring the extremely tiny by observing the extremely huge

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Let's go back in time...



What's in a ν ame?

Language	Word tree	Some branches	Meaning
Physics (Fermi 1934)	NEUTR-INO		Little neutral one 🔥
Italian	NEUTRO		Neutral
Latin	NE-UTER		Not either; neutral
Latin	UTER		Either
Greek	1 _	OUDETEROS	Neutral
Old High German		HWEDAR	Which of two; whether
Phonetic change/loss	[K]UOTER[US]		Which of the two?
Ionic Greek	KOTEROS		Which of the two?
Sanskrit	KATARAS		Which of the two?
Latin	1	QUANTUS	How much?
Sanskrit		KATAMAS	Which out of many?
Sanskrit		KATHA	How?
Sanskrit	/	KAS	Who?
Indo-European root	KA or KWA		Interrogative base

Answer: ν 's destiny is to raise kwastions!

Courtesy of Eligio Lisi, Summary Talk (Theory) at Neutrino 2010, Athens

Preliminary Q: why care about neutrinos?

Neutrinos are the only direct evidence for physics beyond the Standard Model

$$-Y^{ij}\bar{\psi}_i\Phi\psi_j = -Y^{ij}_e\bar{E}^i_L\Phi e^j_R - Y^{ij}_d\bar{Q}^i_L\Phi d^j_R - Y^{ij}_u\epsilon^{ab}\bar{Q}^i_{La}\Phi^*_bu^j_R + \text{h.c.}$$

No right-handed neutrino field ν_R in the Standard Model

Overview: Qs (& As)

- Q: What can cosmology tell us about massive neutrinos? A: **Quite a lot**!
- Q: Can you elaborate a bit more?
 A: Cosmology is sensitive to the sum of the three neutrino masses M_ν and gives the tightest upper bounds on this quantity.
- Q: Is that all? Can it tell us something about the mass hierarchy? A: **Yes, if one is careful...**
- Q: I heard there's some connection between νs and dark energy...?
 A: Yes, νs could shed light on what is (not) driving cosmic acceleration!
- Q: How does the future of neutrino cosmology look? A: VERY EXCITING!!!

The Standard Cosmological Model



The Cosmic Neutrino Background (C ν B)

- The presence of a background of relic neutrinos (CνB) is a basic prediction of the standard cosmological model
- Weak interactions maintain ν s in thermal equilibrium with the primeval cosmological plasma until $T \sim 1 \,\mathrm{MeV}~(z \sim 10^{10})$
- Below $T \sim 1 \,\mathrm{MeV} \, \nu$ s free-stream keeping an equilibrium spectrum:

$$f_{\nu}(p,T) = \frac{1}{e^{\frac{p-\mu}{T}}+1}$$

- When the temperature drops below their mass, neutrinos turn non-relativistic, and their free-streaming suppresses the growth of structure on small scales (VERY IMPORTANT)
- Today $T_{
 u}\simeq 1.9\,{
 m K}$, $n_{
 u}\simeq 113\,{
 m cm}^{-3}$, $N_{
 m eff}=3.046$

The Cosmic Neutrino Background ($C\nu B$)

Neutrinos behave as radiation at early times, as matter at late times



Neutrino masses

Nobel Prize 2015: "för upptäckten av neutrinooscillationer, som visar att neutriner har massa" ("for the discovery of neutrino oscillations, which shows that neutrinos have mass")



Neutrinos from the lab

Flavour transition probability:

$$P_{lpha
ightarroweta}\propto\sin^2\left(rac{\Delta m^2 L}{E}
ight)$$

So we have two non-zero $\Delta m^2 \rightarrow$ at least 2 out of 3 mass eigenstates have non-zero mass.

From oscillation experiments accurate measurements of two mass-squared differences:

$$\begin{array}{rcl} \Delta m_{21}^2 &\equiv& m_2^2 - m_1^2 = (7.6 \pm 0.2) \times 10^{-5} \, \mathrm{eV}^2 \,, \\ |\Delta m_{31}^2| &\equiv& |m_3^2 - m_1^2| = (2.48 \pm 0.06) \times 10^{-3} \, \mathrm{eV}^2 \,. \end{array}$$

Note uncertainty in sign of Δm_{31}^2 !!!.

Neutrino mass hierarchy

Oscillation data put a lower limit on the absolute mass scale depending on the mass hierarchy:



$$\begin{split} M_{\nu,\min} &= \sqrt{\Delta m_{21}^2} + \sqrt{\Delta m_{31}^2} \simeq 0.06 \,\mathrm{eV} \,\,(\mathsf{NH}) \\ M_{\nu,\min} &= \sqrt{\Delta m_{31}^2} + \sqrt{\Delta m_{31}^2 + \Delta m_{21}^2} \simeq 0.1 \,\mathrm{eV} \,\,(\mathsf{IH}) \end{split}$$

Neutrino unknowns

- Absolute mass scale $M_{
 u}\equiv\sum_{i}m_{
 u_{i}}$
- Mass hierarchy
- θ_{23} octant
- Dirac vs Majorana nature
- CP violation
- Sterile eigenstates

Neutrino oscillations

- Sensitive to mass-squared differences $\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$
- Exploits quantum-mechanical effects
- Currently not sensitive to the mass hierarchy

Cosmology

- Sensitive to sum of neutrino masses $M_{\nu} \equiv \sum_{i} m_{i}$
- Exploits GR+Boltzmann equations
- Tightest limits, but somewhat model-dependent



Beta decay

- Sensitive to effective electron neutrino mass $m_{\beta}^2 \equiv \sum_i |U_{ei}|^2 m_i^2$
- Exploits conservation of energy
- Model-independent, but less tight bounds



Neutrinoless double-beta decay

- Sensitive to effective Majorana mass $m_{\beta\beta}\equiv \sum_i |U_{e_i}^2 m_i|$
- Exploits 0ν2β decay (if νs are Majorana)
- Limited by NME uncertainties and u nature



How can cosmology measure neutrino masses?



Courtesy of Martina Gerbino

Cosmological datasets: Cosmic Microwave Background



Credits: Planck collaboration

Cosmological datasets: CMB lensing

CMB photons deflected according to the deflection field $\vec{d} = \vec{\nabla}\phi$, with lensing potential ϕ given by:

$$\phi = -\int_0^{\chi^*} d\chi \; \frac{\chi^* - \chi}{\chi^* \chi} (\Phi + \Psi)$$



Cosmological datasets: CMB lensing



Credits: Planck collaboration

Cosmological datasets: CMB spectra



Note: red curve obtained from 6-parameter ACDM model fit to TT only

CMB temperature power spectrum



- Small ℓ (large angular scales): late ISW plateau
- $\ell \approx 200$: first acoustic peak carries a lot of cosmological information
- $\ell\gtrsim$ 500: damped acoustic peaks (*Silk damping*), but damping is smeared by gravitational lensing

Effect of neutrino masses on the CMB: background level

• Shift in matter-radiation equality redshift:

$$1 + z_{\rm eq} = \frac{\Omega_b + \Omega_{cdm}}{\Omega_\gamma \left[1 + \frac{7}{8} \left(\frac{4}{11}\right)^{\frac{4}{3}} N_{\rm eff}\right]}$$

Affects height of first peak through early ISW effect

• Shift in distance to the CMB:

$$d_A(z_{
m CMB}) \propto rac{1}{H_0} \int_0^{z_{
m CMB}} rac{dz}{\sqrt{(\Omega_b + \Omega_{cdm})(1+z)^3 + \Omega_\Lambda + \Omega_
u(z)}}$$

Affects position of first peak, since:

$$\ell_{
m peak}\simeq rac{\pi}{ heta_{
m peak}}\,,\quad heta_{
m peak}pprox rac{r_{s}(z_{
m CMB})}{d_{A}(z_{
m CMB})}$$

These effects were the ones mainly driving the WMAP bound ($M_{\nu} < 0.1\,{\rm eV}$ @95% C.L.)

Effect of neutrino masses on the CMB: perturbation level

- Massive neutrinos free-streaming damps small-scale perturbations...
- ...less structure=less lensing=less smearing of the small-scale power spectrum of the CMB (Planck: $M_{\nu} < 0.72 \,\mathrm{eV}$ @95% C.L.)
- Small effect on the late ISW plateau (but large error bars)
- Small changes around the first peak
- Small effect on the damping tail

Effect of neutrino masses on the CMB



Neutrino masses and the large-scale structure

Free-streaming of neutrinos suppresses growth of structure on small scales and hence **matter** power spectrum



On small scales (large k), where the suppression is maximal:

$$rac{\Delta P_m(k)}{P_m(k)}\sim -8f_
u\,,\quad f_
u\equiv rac{\Omega_
u}{\Omega_m}$$

Cosmological data: galaxy redshift surveys

Sloan Digital Sky Survey (SDSS) - Baryon Oscillation Spectroscopic Survey (BOSS)



Essentially get two types of measurements out:

- Galaxy power spectrum P(k): measurement of amount of clustering
- Baryon Acoustic Oscillation (BAO): distance measurement

Galaxy power spectrum



Issues:

• (Scale-dependent) bias

 $P_g(k) = b^2(k)P_m(k)$

 $P_m(k)$: what we would like to measure

- $P_g(k)$: what we measure $b^2(k)$: what makes life hard
- Non-linearities
- Redshift-space distortions
- Systematics

Baryon Acoustic Oscillations



Approximately constrain the quantity $D_v(z_{\text{eff}})/r_s(z_{\text{drag}})$, where:

$$D_{v}(z) = \left[(1+z)^{2} D_{A}(z)^{2} \frac{cz}{H(z)} \right]^{\frac{1}{3}}$$

Standard ruler

• Substantially less affected by bias, non-linear evolution, than P(k)

Cosmological data: other types of data

- Measurement of optical depth to reionization $\tau = 0.055 \pm 0.009$ (proxy for *Planck* 2018 final data release)
- Direct measurements of H_0 from HST
- Sunyaev-Zel'dovich cluster counts
- Redshift-space distortions measurements from galaxy redshift surveys
- Weak lensing measurements (CFHTLens, KiDS, Euclid)
- Supernovae la luminosity distance measurements (JLA, Pantheon)
- Cosmic chronometers
- Lyman- α forest power spectrum (BOSS, eBOSS)
- In the future: 21-cm intensity mapping (SKA)

Things to be aware about: degeneracies



Example: geometrical degeneracy

$$d_{
m CMB} \propto rac{1}{H_0} \int_0^{z_{
m CMB}} rac{dz}{\sqrt{(\Omega_b + \Omega_{cdm})(1+z)^3 + \Omega_\Lambda + \Omega_
u(z, M_
u) + \Omega_k(1+z)^2}}$$

Things to be aware about: tensions



- H₀ CMB vs local measurements
- $\sigma_8 \sqrt{\Omega_m}$ CMB vs weak lensing
- Lyman- α with pretty much everything else



Analysis method

Bayes' theorem (datasets=x, cosmological parameters= θ):

 $p(heta|\mathbf{x}) \propto \mathcal{L}(\mathbf{x}|m{ heta})\mathcal{P}(m{ heta})$

- $p(\theta)$: posterior (what you want to get)
- $\mathcal{L}(\mathbf{x}|\boldsymbol{ heta})$: likelihood (easy to model, hard to code up)
 - $\mathcal{P}(\boldsymbol{\theta})$: prior (what you have to choose)

Vary 6 basic cosmological parameters $\Omega_b h^2$, $\Omega_c h^2$, Θ_s , τ , n_s , $\log(10^{10}A_s) + M_{\nu} + many$ other nuisance parameters, sample posterior using Markov chain Monte Carlo (MCMC) techniques

Note: cosmology is only sensitive to the sum of the neutrino masses M_{ν} , not to the masses of the individual eigenstates

Report 95% C.L. upper limit on M_{ν} , M_{95} , such that:

$$\frac{\int_{M_0}^{M_{95}} dM_{\nu} \ p(M_{\nu}|\mathbf{x})}{\int_{M_0}^{\infty} dM_{\nu} \ p(M_{\nu}|\mathbf{x})} = 0.95$$

Recap: neutrino mass hierarchy



Results: overview

SV et al., arXiv: 1701.08172

 $\begin{array}{l} \textit{Planck temperature} \\ \textit{M}_{\nu} < \textbf{0.72}\,\mathrm{eV} ~\texttt{095\% C.L.} \end{array}$

- +*P*(*k*): **0.30** eV
- +*P*(*k*)+BAO: **0.19** eV
- +*P*(*k*)+BAO+*τ*: **0.15** eV
- +P(k)+BAO+H₀: 0.15 eV
- $+P(k)+BAO+H_0+\tau$: **0.12** eV

 $\begin{array}{l} \textit{Planck} \text{ temperature+polarization} \\ \textit{M}_{\nu} < \textbf{0.49}\,\mathrm{eV} ~\texttt{@95\%} ~\texttt{C.L.} \end{array}$

• +*P*(*k*): **0.28** eV

- +*P*(*k*)+BAO: **0.15** eV
- +*P*(*k*)+BAO+*τ*: **0.12** eV
- +*P*(*k*)+BAO+*H*₀: 0.11 eV
- $+P(k)+BAO+H_0+\tau$: **0.09** eV

These are the tightest bounds on M_{ν} ever derived in the literature!

Constraints on M_{ν} : take home messages

- Bounds on M_{ν} from cosmology are **VERY** strong (compare to $M_{\nu} \lesssim 2 \, {\rm eV}$ from β -decay)
- A robust 95% C.L. upper bound is about $M_{
 u} \lesssim 0.15\,{
 m eV}$
- We are approaching the region of parameter space where the inverted hierarchy is **disfavored**



How to improve from here? Measuring the scale-dependent bias

What we measure $\rightarrow P_g(k) = b^2(k)P_m(k) \leftarrow$ What we would like to measure

Idea: Giusarma, SV, et al., arXiv: 1802.08694

• cross-correlate CMB lensing with galaxy survey!

$$C_{\ell}^{\kappa g} = \frac{3H_0^2\Omega_m}{2c^2} \int_{z_1}^{z_2} dz \ \frac{\chi^{\star} - \chi(z)}{\chi(z)\chi^{\star}} (1+z) b\left(k = \frac{\ell}{\chi(z)}\right) P_m\left(\frac{\ell}{\chi(z)}, z\right) \propto b^1$$

• Use a well-motivated form for the bias: $b(k) = a + ck^2$ Desjacques et al., arXiv: 1611.09787

Results:

- Factor of ≈ 2 improvement in constraints! Upper limit with Planck temperature+P(k) improves from 0.3 eV to 0.15 eV
- Better treatment of non-linearities

A complication: neutrino-induced scale-dependent bias

Neutrinos induce an additional scale-dependence in the bias (always neglected) Castorina et al., arXiv: 1311.1212

 $P_g(k) = b^2(k, M_\nu) P_m(k)$

Problem: $b^2(k, M_{\nu})$ hard to model

Solution: define the bias with respect to CDM+baryons **only**

 $P_g(k) = b_{cb}^2(k) P_{cb}(k)$

The bias $b_{cb}(k)$ no longer depends on $M_{\nu}!$



Brinckmann, SV, et al., paper in preparation (2018)

What can cosmology say about the mass hierarchy?

- Cosmology is sensitive to $M_{
 u}=m_1+m_2+m_3$, not to the m_i s...
- For each mass hierarchy, there exists a minimal allowed value for $M_{\nu}...$
- ...so näively you would say that if we set a limit $M_{\nu} < 0.1 \,\mathrm{eV}$ we know the neutrino hierarchy is normal! (and have a paper in *Nature/Science/PRL*)



What can cosmology say about the mass hierarchy?

- What we really have to solve is a **Bayesian model selection** problem between two models: normal hierarchy (NH) and inverted hierarchy (IH)
- In other words, compute **posterior odds** for normal vs inverted hierarchy, *after having observed cosmological data*:

$$\frac{p_{\rm NH}}{p_{\rm IH}} \approx \frac{\int_{0.06 \, {\rm eV}}^{\infty} dM_{\nu} \, p(M_{\nu} | \mathbf{x}) \mathcal{P}(M_{\nu})}{\int_{0.10 \, {\rm eV}}^{\infty} dM_{\nu} \, p(M_{\nu} | \mathbf{x}) \mathcal{P}(M_{\nu})}$$

where $p(M_{\nu}|\mathbf{x})$ is your posterior distribution and $\mathcal{P}(M_{\nu})$ your prior distribution SV et al., arXiv: 1701.08172, different formulation leading to approximately same answer in Hannestad & Schwetz. arXiv: 1606.04691

• Note that $\mathcal{P}(M_{\nu})$ appears: dependence on how you weigh your prior volume \rightarrow preference for normal hierarchy driven not by physical effects but **volume effects**

What can cosmology say about the mass hierarchy?

- Even for the most constraining data combination ($M_{\nu} < 0.09 \,\mathrm{eV}$), $p_{\mathrm{NH}} : p_{\mathrm{IH}} \sim 3.3 : 1$, inverted hierarchy excluded at 77% C.L.
- All sensitivity to the mass hierarchy is entirely due to volume effects, i.e. the possibility of excluding the region above $0.1\,{\rm eV}$ at increasing confidence level
- Recent claims of huge preference (42:1, 95:1, >100:1) for normal hierarchy... Simpson et al., arXiv: 1703.03425
- ...result of "weird" (unphysical) choice of prior $\mathcal{P}(M_{\nu})$ See rebuttal paper, Schwetz et al. (incl. SV), arXiv: 1703.04585
- Other papers have explored other physical priors/methodologies, but preference for normal hierarchy is never > 5 : 1

Constraints on mass hierarchy: take home messages

- There is a weak preference ($\sim 2:1)$ for the NH from cosmology
- $\bullet\,$ Even with the least conservative datasets at most $\sim3:1$ preference
- All preference for the NH is driven by volume effects (i.e. at what significance I can exclude the region $>0.1\,{\rm eV})$
- Corollary of the above: be careful how you weigh your prior volume!



Model-dependency of cosmology bounds

The bounds so far assumed a background Λ CDM model, i.e. only 6 parameters. Introducing other parameters **degrades** the bound on M_{ν}

Planck temperature + BAO assuming Λ CDM: $M_{\nu} < 0.25 \, \mathrm{eV}$

- < 0.37 m eV if allow curvature Ω_k to vary ($\Omega_k=$ 0 in ACDM)
- < 0.37 m eV if allow dark energy EoS w to vary (w = -1 in ACDM)
- In modified gravity models you can get a **detection** of non-zero M_{ν} instead of an upper bound (e.g. cubic/quartic/quintic Galileon gravity, $M_{\nu} \simeq (0.51 \pm 0.19) \, {\rm eV})$ Renk et al., arXiv: 1707.02263
- ...several other possible examples including evolving dark energy, effective number of neutrino species, tensor-to-scalar ratio, running of scalar spectral index, primordial Helium fraction, lensing amplitude

Although most of these extensions are *statistically disfavoured* from a Bayesian evidence point of view (**Occam's razor**) Heavens et al., arXiv: 1704.03467

Model-dependency of cosmology bounds

Why do the bounds degrade? **Degeneracies**, again! M_{ν} -w example:



$$d_{\rm CMB} \propto \int \frac{dz}{\sqrt{(\Omega_b + \Omega_{cdm})(1+z)^3 + \Omega_{\rm DE}(z,w) + \Omega_\nu(z,M_\nu)}}\,, \quad \frac{d\Omega_{\rm DE}}{dw} < 0\,, \quad \frac{d\Omega_\nu}{dM_\nu} > 0$$

Single, minimally-coupled scalar ϕ , with canonical kinetic term

Ratra & Peebles 1988; Wetterich 1988; Caldwell, Dave & Steinhardt 1998

$${\cal L}_{\phi}=-rac{1}{2}\partial^{\mu}\phi\partial_{\mu}\phi-V(\phi)$$

Pressure and energy density:

$$ho_{\phi} = rac{1}{2} \dot{\phi}^2 + V(\phi) \,, \quad P_{\phi} = rac{1}{2} \dot{\phi}^2 - V(\phi)$$

Equation of state is **non-phantom**:

$$w_{\phi} = rac{P_{\phi}}{
ho_{\phi}} = rac{rac{1}{2}\dot{\phi}^2 - V(\phi)}{rac{1}{2}\dot{\phi}^2 + V(\phi)} \geq -1$$

At the cosmological level well modelled as Linder, arXiv: 0704.2064, SV et al., arXiv: 1801.08553

$$w(z) = w_0 + w_a \frac{z}{1+z}, \quad \mathbf{w_0} \ge -\mathbf{1}, \quad \mathbf{w_0} + \mathbf{w_a} \ge -\mathbf{1} \to w(z) \ge -1 \,\forall z$$

In quintessence (and more generally non-phantom dark energy) models the bounds on M_{ν} become $\approx 25\%$ tighter than in Λ CDM despite having more parameters SV et al., arXiv: 1801.08553





Implications: SV et al., arXiv: 1801.08553

- In non-phantom dark energy models the preference for the normal neutrino hierarchy is significantly stronger ($\approx 3-4:1$) than in Λ CDM ($\approx 2:1$)
- If independent laboratory experiments measure the hierarchy to be inverted, we can be almost sure dark energy is phantom (→ Big Rip?) → insight into the nature of dark energy/cosmic acceleration from neutrino laboratory measurements
- Similar considerations might apply to certain modified gravity models
- Similar exception happens in other extended models (e.g. negative curvature, low-scale reheating, negative running), currently being examined → insight into extremely early Universe physics from neutrino laboratory measurements SV et al., paper in preparation (2018)

The future of neutrino cosmology

- Future CMB experiments (improvements especially in lensing): e.g. Advanced ACTPol, SPT-3G, Simons Observatory, CMB-S4
- Future cluster surveys
- Future galaxy surveys: e.g. eBOSS, DESI, LSST, WFIRST
- Galaxy weak lensing (cosmic shear): e.g. Euclid
- \bullet Lyman α power spectrum: can probe very small scales
- 21-cm intensity mapping: e.g. SKA

The future of neutrino cosmology

Q: what do future cosmological surveys have in store for ν s?



	$\sigma (\sum m_{\nu}) \text{ [meV]}$
CMB Lensing (current galaxy clustering):	
Stage-IV CMB	45
Stage-IV CMB + BOSS BAO	25
CMB Lensing + Galaxy clustering:	
Stage-IV CMB + eBOSS BAO	23
Stage-IV CMB + DESI BAO	16
Stage-IV CMB no lensing + DESI galaxy clustering	15/20
Galaxy Weak Lensing:	
Planck + LSST [51]	23
Planck + Euclid [48]	25

Credits: K. Abazajian et al., arXiv:1309.5383

A: a sure detection of M_{ν} and possibly of the mass hierarchy (but only if the detected M_{ν} is substantially smaller than $0.1 \,\mathrm{eV}$)! P.S.: optimists suggest we could measure the individual masses m_i

The future of neutrino cosmology



Allison et al., arXiv: 1509.7471

...and wide time and scale coverage from future data will help breaking degeneracies (e.g. with w, distinguish effects of ν vs dark energy)

Conclusions

- Cosmology provides **tightest** constraints on sum of ν masses, $M_{\nu} \lesssim 0.15 \,\mathrm{eV}$ (assuming ΛCDM)
- Lots of room for improvement (use cross-correlations?), but beware systematic effects (neutrino-induced scale-dependent bias)
- Mild preference for normal hierarchy due to volume effects → beware your choice of prior!
- Upper limits on M_{ν} usually degrade when relaxing assumptions on underlying cosmology \rightarrow model-dependence
- An important exception: **non-phantom dark energy** (quintessence) $\rightarrow \nu$ lab experiments illuminate the nature of dark energy?
- The future of ν cosmology is very bright, with a **detection** of M_{ν} and possibly the hierarchy expected within the next years: stay tuned!

What's in a ν ame?

Language	Word tree	Some branches	Meaning
Physics (Fermi 1934)	NEUTR-INO		Little neutral one
Italian	NEUTRO		Neutral
Latin	NE-UTER		Not either; neutral
Latin	UTER		Either
Greek	1	OUDETEROS	Neutral
Old High German		HWEDAR	Which of two; whether
Phonetic change/loss	[K]UOTER[US]		Which of the two?
Ionic Greek	KOTEROS		Which of the two?
Sanskrit	KATARAS		Which of the two?
Latin	^	QUANTUS	How much?
Sanskrit		KATAMAS	Which out of many?
Sanskrit		KATHA	How?
Sanskrit		KAS	Who?
Indo-European root	KA or KWA		Interrogative base